

# Worksheet

05/07/2020

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Problem quickname: 2001

1)

Determine the greatest common divisor (GCD). Use the Euclidean Algorithm and write down the computational steps in detail.

Quick:  
2001

- a) Number 1: 24, Number 2: 28. Determine the larger number of these: 28.

Round 1:

Determine the quotient and remainder of  $28 : 24$ .

We have  $28 = 1 \cdot 24 + 4$ , so the quotient is 1, the remainder is 4.

Now select the divisor 24 of this round as new dividend and the remainder 4 as new divisor.

Round 2:

Determine the quotient and remainder of  $24 : 4$ .

We have  $24 = 6 \cdot 4 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 4 is also the GCD, so we have  $\gcd(28,24)=4$ .

- b) Number 1: 77, Number 2: 55. Determine the larger number of these: 77.

Round 1:

Determine the quotient and remainder of  $77 : 55$ .

We have  $77 = 1 \cdot 55 + 22$ , so the quotient is 1, the remainder is 22.

Now select the divisor 55 of this round as new dividend and the remainder 22 as new divisor.

Round 2:

Determine the quotient and remainder of  $55 : 22$ .

We have  $55 = 2 \cdot 22 + 11$ , so the quotient is 2, the remainder is 11.

Now select the divisor 22 of this round as new dividend and the remainder 11 as new divisor.

Round 3:

Determine the quotient and remainder of  $22 : 11$ .

We have  $22 = 2 \cdot 11 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 11 is also the GCD, so we have  $\gcd(77,55)=11$ .

- c) Number 1: 54, Number 2: 27. Determine the larger number of these: 54.

Round 1:

Determine the quotient and remainder of  $54 : 27$ .

We have  $54 = 2 \cdot 27 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 27 is also the GCD, so we have  $\gcd(54,27)=27$ .

- d) Number 1: 72, Number 2: 52. Determine the larger number of these: 72.

Round 1:

Determine the quotient and remainder of  $72 : 52$ .

We have  $72 = 1 \cdot 52 + 20$ , so the quotient is 1, the remainder is 20.

Now select the divisor 52 of this round as new dividend and the remainder 20 as new divisor.

Round 2:

Determine the quotient and remainder of  $52 : 20$ .

We have  $52 = 2 \cdot 20 + 12$ , so the quotient is 2, the remainder is 12.

Now select the divisor 20 of this round as new dividend and the remainder 12 as new divisor.

Round 3:

Determine the quotient and remainder of  $20 : 12$ .

We have  $20 = 1 \cdot 12 + 8$ , so the quotient is 1, the remainder is 8.

Now select the divisor 12 of this round as new dividend and the remainder 8 as new divisor.

Round 4:

Determine the quotient and remainder of  $12 : 8$ .

We have  $12 = 1 \cdot 8 + 4$ , so the quotient is 1, the remainder is 4.

Now select the divisor 8 of this round as new dividend and the remainder 4 as new divisor.

Round 5:

Determine the quotient and remainder of  $8 : 4$ .

We have  $8 = 2 \cdot 4 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 4 is also the GCD, so we have  $\gcd(72,52)=4$ .

- e) Number 1: 21, Number 2: 52. Determine the larger number of these: 52.

Round 1:

Determine the quotient and remainder of  $52 : 21$ .

We have  $52 = 2 \cdot 21 + 10$ , so the quotient is 2, the remainder is 10.

Now select the divisor 21 of this round as new dividend and the remainder 10 as new divisor.

Round 2:

Determine the quotient and remainder of  $21 : 10$ .

We have  $21 = 2 \cdot 10 + 1$ , so the quotient is 2, the remainder is 1.

Now select the divisor 10 of this round as new dividend and the remainder 1 as new divisor.

Round 3:

Determine the quotient and remainder of  $10 : 1$ .

We have  $10 = 10 \cdot 1 + 0$ , so the quotient is 10, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\gcd(52,21)=1$ .

- f) Number 1: 91, Number 2: 70. Determine the larger number of these: 91.

Round 1:

Determine the quotient and remainder of  $91 : 70$ .

We have  $91 = 1 \cdot 70 + 21$ , so the quotient is 1, the remainder is 21.

Now select the divisor 70 of this round as new dividend and the remainder 21 as new divisor.

Round 2:

Determine the quotient and remainder of  $70 : 21$ .

We have  $70 = 3 \cdot 21 + 7$ , so the quotient is 3, the remainder is 7.

Now select the divisor 21 of this round as new dividend and the remainder 7 as new divisor.

Round 3:

Determine the quotient and remainder of  $21 : 7$ .

We have  $21 = 3 \cdot 7 + 0$ , so the quotient is 3, the remainder is 0.

Finished. The last dividend 7 is also the GCD, so we have  $\gcd(91,70)=7$ .

g) Number 1: 28, Number 2: 91. Determine the larger number of these: 91.

Round 1:

Determine the quotient and remainder of  $91 : 28$ .

We have  $91 = 3 \cdot 28 + 7$ , so the quotient is 3, the remainder is 7.

Now select the divisor 28 of this round as new dividend and the remainder 7 as new divisor.

Round 2:

Determine the quotient and remainder of  $28 : 7$ .

We have  $28 = 4 \cdot 7 + 0$ , so the quotient is 4, the remainder is 0.

Finished. The last dividend 7 is also the GCD, so we have  $\text{gcd}(91,28)=7$ .

2)

Determine the greatest common divisor (GCD). Use the Euclidean Algorithm as shown in the example. Write down the computational steps in detail.

Quick:  
2001

a) Number 1: 55, Number 2: 48. Determine the larger number of these: 55.

Round 1:

Determine the quotient and remainder of  $55 : 48$ .

We have  $55 = 1 \cdot 48 + 7$ , so the quotient is 1, the remainder is 7.

Now select the divisor 48 of this round as new dividend and the remainder 7 as new divisor.

Round 2:

Determine the quotient and remainder of  $48 : 7$ .

We have  $48 = 6 \cdot 7 + 6$ , so the quotient is 6, the remainder is 6.

Now select the divisor 7 of this round as new dividend and the remainder 6 as new divisor.

Round 3:

Determine the quotient and remainder of  $7 : 6$ .

We have  $7 = 1 \cdot 6 + 1$ , so the quotient is 1, the remainder is 1.

Now select the divisor 6 of this round as new dividend and the remainder 1 as new divisor.

Round 4:

Determine the quotient and remainder of  $6 : 1$ .

We have  $6 = 6 \cdot 1 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\text{gcd}(55,48)=1$ .

- b) Number 1: 64, Number 2: 46. Determine the larger number of these: 64.

Round 1:

Determine the quotient and remainder of  $64 : 46$ .

We have  $64 = 1 \cdot 46 + 18$ , so the quotient is 1, the remainder is 18.

Now select the divisor 46 of this round as new dividend and the remainder 18 as new divisor.

Round 2:

Determine the quotient and remainder of  $46 : 18$ .

We have  $46 = 2 \cdot 18 + 10$ , so the quotient is 2, the remainder is 10.

Now select the divisor 18 of this round as new dividend and the remainder 10 as new divisor.

Round 3:

Determine the quotient and remainder of  $18 : 10$ .

We have  $18 = 1 \cdot 10 + 8$ , so the quotient is 1, the remainder is 8.

Now select the divisor 10 of this round as new dividend and the remainder 8 as new divisor.

Round 4:

Determine the quotient and remainder of  $10 : 8$ .

We have  $10 = 1 \cdot 8 + 2$ , so the quotient is 1, the remainder is 2.

Now select the divisor 8 of this round as new dividend and the remainder 2 as new divisor.

Round 5:

Determine the quotient and remainder of  $8 : 2$ .

We have  $8 = 4 \cdot 2 + 0$ , so the quotient is 4, the remainder is 0.

Finished. The last dividend 2 is also the GCD, so we have  $\gcd(64,46)=2$ .

- c) Number 1: 21, Number 2: 39. Determine the larger number of these: 39.

Round 1:

Determine the quotient and remainder of  $39 : 21$ .

We have  $39 = 1 \cdot 21 + 18$ , so the quotient is 1, the remainder is 18.

Now select the divisor 21 of this round as new dividend and the remainder 18 as new divisor.

Round 2:

Determine the quotient and remainder of  $21 : 18$ .

We have  $21 = 1 \cdot 18 + 3$ , so the quotient is 1, the remainder is 3.

Now select the divisor 18 of this round as new dividend and the remainder 3 as new divisor.

Round 3:

Determine the quotient and remainder of  $18 : 3$ .

We have  $18 = 6 \cdot 3 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\gcd(39,21)=3$ .

- d) Number 1: 42, Number 2: 48. Determine the larger number of these: 48.

Round 1:

Determine the quotient and remainder of  $48 : 42$ .

We have  $48 = 1 \cdot 42 + 6$ , so the quotient is 1, the remainder is 6.

Now select the divisor 42 of this round as new dividend and the remainder 6 as new divisor.

Round 2:

Determine the quotient and remainder of  $42 : 6$ .

We have  $42 = 7 \cdot 6 + 0$ , so the quotient is 7, the remainder is 0.

Finished. The last dividend 6 is also the GCD, so we have  $\gcd(48,42)=6$ .

- e) Number 1: 68, Number 2: 59. Determine the larger number of these: 68.

Round 1:

Determine the quotient and remainder of  $68 : 59$ .

We have  $68 = 1 \cdot 59 + 9$ , so the quotient is 1, the remainder is 9.

Now select the divisor 59 of this round as new dividend and the remainder 9 as new divisor.

Round 2:

Determine the quotient and remainder of  $59 : 9$ .

We have  $59 = 6 \cdot 9 + 5$ , so the quotient is 6, the remainder is 5.

Now select the divisor 9 of this round as new dividend and the remainder 5 as new divisor.

Round 3:

Determine the quotient and remainder of  $9 : 5$ .

We have  $9 = 1 \cdot 5 + 4$ , so the quotient is 1, the remainder is 4.

Now select the divisor 5 of this round as new dividend and the remainder 4 as new divisor.

Round 4:

Determine the quotient and remainder of  $5 : 4$ .

We have  $5 = 1 \cdot 4 + 1$ , so the quotient is 1, the remainder is 1.

Now select the divisor 4 of this round as new dividend and the remainder 1 as new divisor.

Round 5:

Determine the quotient and remainder of  $4 : 1$ .

We have  $4 = 4 \cdot 1 + 0$ , so the quotient is 4, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\gcd(68,59)=1$ .

f) Number 1: 77, Number 2: 66. Determine the larger number of these: 77.

Round 1:

Determine the quotient and remainder of  $77 : 66$ .

We have  $77 = 1 \cdot 66 + 11$ , so the quotient is 1, the remainder is 11.

Now select the divisor 66 of this round as new dividend and the remainder 11 as new divisor.

Round 2:

Determine the quotient and remainder of  $66 : 11$ .

We have  $66 = 6 \cdot 11 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 11 is also the GCD, so we have  $\gcd(77,66)=11$ .

g) Number 1: 68, Number 2: 27. Determine the larger number of these: 68.

Round 1:

Determine the quotient and remainder of  $68 : 27$ .

We have  $68 = 2 \cdot 27 + 14$ , so the quotient is 2, the remainder is 14.

Now select the divisor 27 of this round as new dividend and the remainder 14 as new divisor.

Round 2:

Determine the quotient and remainder of  $27 : 14$ .

We have  $27 = 1 \cdot 14 + 13$ , so the quotient is 1, the remainder is 13.

Now select the divisor 14 of this round as new dividend and the remainder 13 as new divisor.

Round 3:

Determine the quotient and remainder of  $14 : 13$ .

We have  $14 = 1 \cdot 13 + 1$ , so the quotient is 1, the remainder is 1.

Now select the divisor 13 of this round as new dividend and the remainder 1 as new divisor.

Round 4:

Determine the quotient and remainder of  $13 : 1$ .

We have  $13 = 13 \cdot 1 + 0$ , so the quotient is 13, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\gcd(68,27)=1$ .

3)

Determine the greatest common divisor (GCD). Use the Euclidean Algorithm as shown in the example. Write down the computational steps in detail.

Quick:  
2001

a) Number 1: 351, Number 2: 969. Determine the larger number of these: 969.

Round 1:

Determine the quotient and remainder of  $969 : 351$ .

We have  $969 = 2 \cdot 351 + 267$ , so the quotient is 2, the remainder is 267.

Now select the divisor 351 of this round as new dividend and the remainder 267 as new divisor.

Round 2:

Determine the quotient and remainder of  $351 : 267$ .

We have  $351 = 1 \cdot 267 + 84$ , so the quotient is 1, the remainder is 84.

Now select the divisor 267 of this round as new dividend and the remainder 84 as new divisor.

Round 3:

Determine the quotient and remainder of  $267 : 84$ .

We have  $267 = 3 \cdot 84 + 15$ , so the quotient is 3, the remainder is 15.

Now select the divisor 84 of this round as new dividend and the remainder 15 as new divisor.

Round 4:

Determine the quotient and remainder of  $84 : 15$ .

We have  $84 = 5 \cdot 15 + 9$ , so the quotient is 5, the remainder is 9.



Now select the divisor 15 of this round as new dividend and the remainder 9 as new divisor.

Round 5:

Determine the quotient and remainder of  $15 : 9$ .

We have  $15 = 1 \cdot 9 + 6$ , so the quotient is 1, the remainder is 6.

Now select the divisor 9 of this round as new dividend and the remainder 6 as new divisor.

Round 6:

Determine the quotient and remainder of  $9 : 6$ .

We have  $9 = 1 \cdot 6 + 3$ , so the quotient is 1, the remainder is 3.

Now select the divisor 6 of this round as new dividend and the remainder 3 as new divisor.

Round 7:

Determine the quotient and remainder of  $6 : 3$ .

We have  $6 = 2 \cdot 3 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\gcd(969,351)=3$ .

b) Number 1: 800, Number 2: 568. Determine the larger number of these: 800.

Round 1:

Determine the quotient and remainder of  $800 : 568$ .

We have  $800 = 1 \cdot 568 + 232$ , so the quotient is 1, the remainder is 232.

Now select the divisor 568 of this round as new dividend and the remainder 232 as new divisor.

Round 2:

Determine the quotient and remainder of  $568 : 232$ .

We have  $568 = 2 \cdot 232 + 104$ , so the quotient is 2, the remainder is 104.

Now select the divisor 232 of this round as new dividend and the remainder 104 as new divisor.

Round 3:

Determine the quotient and remainder of  $232 : 104$ .

We have  $232 = 2 \cdot 104 + 24$ , so the quotient is 2, the remainder is 24.

Now select the divisor 104 of this round as new dividend and the remainder 24 as new divisor.

Round 4:

Determine the quotient and remainder of  $104 : 24$ .

We have  $104 = 4 \cdot 24 + 8$ , so the quotient is 4, the remainder is 8.

Now select the divisor 24 of this round as new dividend and the remainder 8 as new divisor.

Round 5:

Determine the quotient and remainder of  $24 : 8$ .

We have  $24 = 3 \cdot 8 + 0$ , so the quotient is 3, the remainder is 0.

Finished. The last dividend 8 is also the GCD, so we have  $\gcd(800,568)=8$ .

c) Number 1: 620, Number 2: 284. Determine the larger number of these: 620.

Round 1:

Determine the quotient and remainder of  $620 : 284$ .

We have  $620 = 2 \cdot 284 + 52$ , so the quotient is 2, the remainder is 52.

Now select the divisor 284 of this round as new dividend and the remainder 52 as new divisor.

Round 2:

Determine the quotient and remainder of  $284 : 52$ .

We have  $284 = 5 \cdot 52 + 24$ , so the quotient is 5, the remainder is 24.

Now select the divisor 52 of this round as new dividend and the remainder 24 as new divisor.

Round 3:

Determine the quotient and remainder of  $52 : 24$ .

We have  $52 = 2 \cdot 24 + 4$ , so the quotient is 2, the remainder is 4.

Now select the divisor 24 of this round as new dividend and the remainder 4 as new divisor.

Round 4:

Determine the quotient and remainder of  $24 : 4$ .

We have  $24 = 6 \cdot 4 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 4 is also the GCD, so we have  $\gcd(620,284)=4$ .

d) Number 1: 341, Number 2: 875. Determine the larger number of these: 875.

Round 1:

Determine the quotient and remainder of  $875 : 341$ .

We have  $875 = 2 \cdot 341 + 193$ , so the quotient is 2, the remainder is 193.

Now select the divisor 341 of this round as new dividend and the remainder 193 as new divisor.

Round 2:

Determine the quotient and remainder of  $341 : 193$ .

We have  $341 = 1 \cdot 193 + 148$ , so the quotient is 1, the remainder is 148.

Now select the divisor 193 of this round as new dividend and the remainder 148 as new divisor.

Round 3:

Determine the quotient and remainder of  $193 : 148$ .

We have  $193 = 1 \cdot 148 + 45$ , so the quotient is 1, the remainder is 45.

Now select the divisor 148 of this round as new dividend and the remainder 45 as new divisor.

Round 4:

Determine the quotient and remainder of  $148 : 45$ .

We have  $148 = 3 \cdot 45 + 13$ , so the quotient is 3, the remainder is 13.

Now select the divisor 45 of this round as new dividend and the remainder 13 as new divisor.

Round 5:

Determine the quotient and remainder of  $45 : 13$ .

We have  $45 = 3 \cdot 13 + 6$ , so the quotient is 3, the remainder is 6.

Now select the divisor 13 of this round as new dividend and the remainder 6 as new divisor.

Round 6:

Determine the quotient and remainder of  $13 : 6$ .

We have  $13 = 2 \cdot 6 + 1$ , so the quotient is 2, the remainder is 1.

Now select the divisor 6 of this round as new dividend and the remainder 1 as new divisor.

Round 7:

Determine the quotient and remainder of  $6 : 1$ .

We have  $6 = 6 \cdot 1 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\gcd(875,341)=1$ .

- e) Number 1: 921, Number 2: 879. Determine the larger number of these: 921.

Round 1:

Determine the quotient and remainder of  $921 : 879$ .

We have  $921 = 1 \cdot 879 + 42$ , so the quotient is 1, the remainder is 42.

Now select the divisor 879 of this round as new dividend and the remainder 42 as new divisor.

Round 2:

Determine the quotient and remainder of  $879 : 42$ .

We have  $879 = 20 \cdot 42 + 39$ , so the quotient is 20, the remainder is 39.

Now select the divisor 42 of this round as new dividend and the remainder 39 as new divisor.

Round 3:

Determine the quotient and remainder of  $42 : 39$ .

We have  $42 = 1 \cdot 39 + 3$ , so the quotient is 1, the remainder is 3.

Now select the divisor 39 of this round as new dividend and the remainder 3 as new divisor.

Round 4:

Determine the quotient and remainder of  $39 : 3$ .

We have  $39 = 13 \cdot 3 + 0$ , so the quotient is 13, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\text{gcd}(921, 879) = 3$ .

- f) Number 1: 396, Number 2: 981. Determine the larger number of these: 981.

Round 1:

Determine the quotient and remainder of  $981 : 396$ .

We have  $981 = 2 \cdot 396 + 189$ , so the quotient is 2, the remainder is 189.

Now select the divisor 396 of this round as new dividend and the remainder 189 as new divisor.

Round 2:

Determine the quotient and remainder of  $396 : 189$ .

We have  $396 = 2 \cdot 189 + 18$ , so the quotient is 2, the remainder is 18.

Now select the divisor 189 of this round as new dividend and the remainder 18 as new divisor.

Round 3:

Determine the quotient and remainder of  $189 : 18$ .

We have  $189 = 10 \cdot 18 + 9$ , so the quotient is 10, the remainder is 9.

Now select the divisor 18 of this round as new dividend and the remainder 9 as new divisor.

Round 4:

Determine the quotient and remainder of  $18 : 9$ .

We have  $18 = 2 \cdot 9 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 9 is also the GCD, so we have  $\gcd(981, 396) = 9$ .

g) Number 1: 228, Number 2: 915. Determine the larger number of these: 915.

Round 1:

Determine the quotient and remainder of  $915 : 228$ .

We have  $915 = 4 \cdot 228 + 3$ , so the quotient is 4, the remainder is 3.

Now select the divisor 228 of this round as new dividend and the remainder 3 as new divisor.

Round 2:

Determine the quotient and remainder of  $228 : 3$ .

We have  $228 = 76 \cdot 3 + 0$ , so the quotient is 76, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\gcd(915, 228) = 3$ .

4)

Determine the greatest common divisor (GCD). Use the Euclidean Algorithm and write down the computational steps in detail.

a) Number 1: 82, Number 2: 58. Determine the larger number of these: 82.

Round 1:

Determine the quotient and remainder of  $82 : 58$ .

We have  $82 = 1 \cdot 58 + 24$ , so the quotient is 1, the remainder is 24.

Now select the divisor 58 of this round as new dividend and the remainder 24 as new divisor.

Round 2:

Determine the quotient and remainder of  $58 : 24$ .

We have  $58 = 2 \cdot 24 + 10$ , so the quotient is 2, the remainder is 10.

Now select the divisor 24 of this round as new dividend and the remainder 10 as new divisor.

Round 3:

Determine the quotient and remainder of  $24 : 10$ .

We have  $24 = 2 \cdot 10 + 4$ , so the quotient is 2, the remainder is 4.

Now select the divisor 10 of this round as new dividend and the remainder 4 as new divisor.

Round 4:

Determine the quotient and remainder of  $10 : 4$ .

We have  $10 = 2 \cdot 4 + 2$ , so the quotient is 2, the remainder is 2.

Now select the divisor 4 of this round as new dividend and the remainder 2 as new divisor.

Round 5:

Determine the quotient and remainder of  $4 : 2$ .

We have  $4 = 2 \cdot 2 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 2 is also the GCD, so we have  $\gcd(82,58)=2$ .

- b) Number 1: 33, Number 2: 99. Determine the larger number of these: 99.

Round 1:

Determine the quotient and remainder of  $99 : 33$ .

We have  $99 = 3 \cdot 33 + 0$ , so the quotient is 3, the remainder is 0.

Finished. The last dividend 33 is also the GCD, so we have  $\gcd(99,33)=33$ .

- c) Number 1: 86, Number 2: 43. Determine the larger number of these: 86.

Round 1:

Determine the quotient and remainder of  $86 : 43$ .

We have  $86 = 2 \cdot 43 + 0$ , so the quotient is 2, the remainder is 0.

Finished. The last dividend 43 is also the GCD, so we have  $\gcd(86,43)=43$ .

- d) Number 1: 39, Number 2: 57. Determine the larger number of these: 57.

Round 1:

Determine the quotient and remainder of  $57 : 39$ .

We have  $57 = 1 \cdot 39 + 18$ , so the quotient is 1, the remainder is 18.

Now select the divisor 39 of this round as new dividend and the remainder 18 as new divisor.

Round 2:

Determine the quotient and remainder of  $39 : 18$ .

We have  $39 = 2 \cdot 18 + 3$ , so the quotient is 2, the remainder is 3.

Now select the divisor 18 of this round as new dividend and the remainder 3 as new divisor.

Round 3:

Determine the quotient and remainder of  $18 : 3$ .

We have  $18 = 6 \cdot 3 + 0$ , so the quotient is 6, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\text{gcd}(57,39)=3$ .

e) Number 1: 46, Number 2: 97. Determine the larger number of these: 97.

Round 1:

Determine the quotient and remainder of  $97 : 46$ .

We have  $97 = 2 \cdot 46 + 5$ , so the quotient is 2, the remainder is 5.

Now select the divisor 46 of this round as new dividend and the remainder 5 as new divisor.

Round 2:

Determine the quotient and remainder of  $46 : 5$ .

We have  $46 = 9 \cdot 5 + 1$ , so the quotient is 9, the remainder is 1.

Now select the divisor 5 of this round as new dividend and the remainder 1 as new divisor.

Round 3:

Determine the quotient and remainder of  $5 : 1$ .

We have  $5 = 5 \cdot 1 + 0$ , so the quotient is 5, the remainder is 0.

Finished. The last dividend 1 is also the GCD, so we have  $\text{gcd}(97,46)=1$ .

f) Number 1: 75, Number 2: 39. Determine the larger number of these: 75.

Round 1:

Determine the quotient and remainder of  $75 : 39$ .

We have  $75 = 1 \cdot 39 + 36$ , so the quotient is 1, the remainder is 36.

Now select the divisor 39 of this round as new dividend and the remainder 36 as new divisor.

Round 2:

Determine the quotient and remainder of  $39 : 36$ .

We have  $39 = 1 \cdot 36 + 3$ , so the quotient is 1, the remainder is 3.

Now select the divisor 36 of this round as new dividend and the remainder 3 as new divisor.

Round 3:

Determine the quotient and remainder of  $36 : 3$ .

We have  $36 = 12 \cdot 3 + 0$ , so the quotient is 12, the remainder is 0.

Finished. The last dividend 3 is also the GCD, so we have  $\gcd(75,39)=3$ .

g) Number 1: 24, Number 2: 54. Determine the larger number of these: 54.

Round 1:

Determine the quotient and remainder of  $54 : 24$ .

We have  $54 = 2 \cdot 24 + 6$ , so the quotient is 2, the remainder is 6.

Now select the divisor 24 of this round as new dividend and the remainder 6 as new divisor.

Round 2:

Determine the quotient and remainder of  $24 : 6$ .

We have  $24 = 4 \cdot 6 + 0$ , so the quotient is 4, the remainder is 0.

Finished. The last dividend 6 is also the GCD, so we have  $\gcd(54,24)=6$ .

Good Luck!